SOLUTIONS

PROBLEM: AP-9

GIVEN:

A particle is moving along a circular path having a radius
of 4 in. such that its position as a function of time is given
by $\theta = \cos 2t$, where θ is in radians and t is in seconds.
Determine the magnitude of the acceleration of the particle
when $\theta = 30°$.

$\theta = 30°$
$= \dfrac{\pi}{6}$

REQUIRED:

$|a|$

SOLUTION:

$r = 4 \text{ in}$ $\dot{r} = 0$ $\ddot{r} = 0$

$\theta = \cos 2t$ $t = 0.510 \text{ s}$

$\dot{\theta} = -\sin 2t (2) = -1.70 \text{ RAD/s}$ $\left\}\begin{array}{l}\theta = 30° \\ t = 0.51 \text{ s}\end{array}\right.$

$\ddot{\theta} = -2\cos 2t (2) = -2.09 \text{ RAD/s2}$

$a_r = -11.61 \text{ IN/s2}$

$a_\theta = -8.38 \text{ IN/s2}$

$\vec{a} = \{-11.61 \, \hat{e}_r - 8.38 \, \hat{e}_\theta\} \frac{\text{IN}}{\text{s2}}$

$a = \sqrt{\Sigma^2} = 14.3 \text{ IN/s2}$

$\boxed{|a| = 14.3 \text{ IN/s2}}$